

## Discrete Mathematics I Assignment 6 (December 07, 2005)

(This assignment is due on December 14, 2005, 1.00 p.m., by dropping it into the wooden box in front of F 310)

### Exercise 1 (Modular arithmetic):

Show that if  $n|m$ , where  $n$  and  $m$  are positive integers greater than 1, and if  $a \equiv b \pmod{m}$ , where  $a$  and  $b$  are integers, then  $a \equiv b \pmod{n}$

(20 Points)

### Exercise 2 (Pseudorandom numbers):

What sequence of pseudorandom numbers is generated using the linear congruential generator  $x_{n+1} = (4x_n + 1) \pmod{7}$  with seed  $x_0 = 3$ ?

(20 Points)

### Exercise 3 (Systems of linear congruences):

- a) Find an  $x \neq 8$  that satisfies  $x \equiv 2 \pmod{3}$  AND  $x \equiv 3 \pmod{5}$ .
- b) Find an  $x$  that satisfies  $x \equiv 7 \pmod{4}$ ,  $x \equiv 2 \pmod{3}$  AND  $x \equiv 5 \pmod{11}$ .

(8+12 Points)