
Collaborative transmission in wireless sensor networks

Alternative algorithmic approaches

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Overview and Structure

- Introduction to context aware computing
- Wireless sensor networks
- Wireless communications
- Basics of probability theory
- Randomised search approaches
- Cooperative transmission schemes
- Distributed adaptive beamforming
 - Feedback based approaches
 - Asymptotic bounds on the synchronisation time
 - Alternative algorithmic approaches
 - Alternative Optimisation environments

Overview and Structure

- Introduction to context aware computing
- Wireless sensor networks
- Wireless communications
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- Cooperative transmission schemes
- **Feedback based distributed adaptive beamforming**
 - Feedback based approaches
 - Asymptotic bounds on the synchronisation time
 - **Alternative algorithmic approaches**
 - Alternative Optimisation environments

Outline

Alternative beamforming approaches

- 1 Hierarchical clustering
- 2 Local random search
- 3 An asymptotically optimal algorithm
- 4 Environmental changes
 - Velocity of nodes
 - Multiple receiver nodes
 - Increased population size
 - Receive beamforming

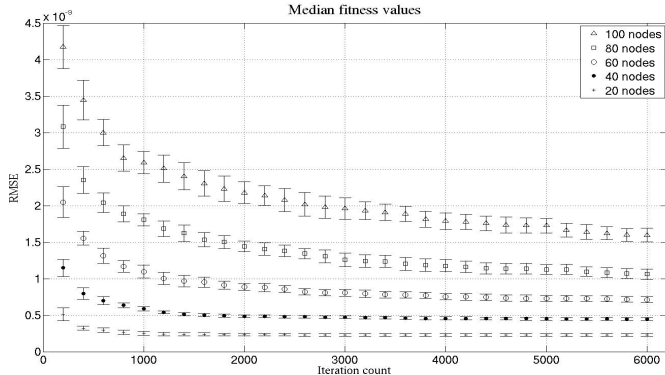
Alternative algorithmic approaches

Hierarchical clustering

- For feedback based distributed adaptive transmit beamforming:
 - RSS_{sum} changes linear with the network size n .
 - Bound on the synchronisation time is more than linear in n

Alternative algorithmic approaches

Hierarchical clustering



$$E[T_{\mathcal{P}}] = \Theta(n \cdot k \cdot \log(n))$$

Alternative algorithmic approaches

Hierarchical clustering

- Hierarchical clustering
 - 1 Determine clusters
 - 2 Synchronise clusters successively (with possibly increased transmit power for nodes)
 - 3 Build and synchronise overlay-cluster of representative nodes from all clusters.
 - 4 Nodes alter carrier phase by phase offset experienced by representative node:

- $\zeta_i = \Re \left(m(t) \text{RSS}_i e^{j2\pi f_c t (\gamma_i + \phi_i + \psi_i)} \right)$ (before)

- $\zeta'_i = \Re \left(m(t) \text{RSS}_i e^{j2\pi f_c t (\gamma'_i + \phi_i + \psi_i)} \right)$ (after)

Node h from same cluster alters carrier signal

- $\zeta_h = \Re \left(m(t) \text{RSS}_h e^{j2\pi f_c t (\gamma_h + \phi_h + \psi_h)} \right)$ to

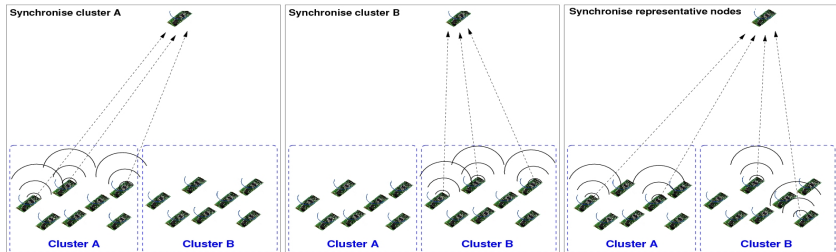
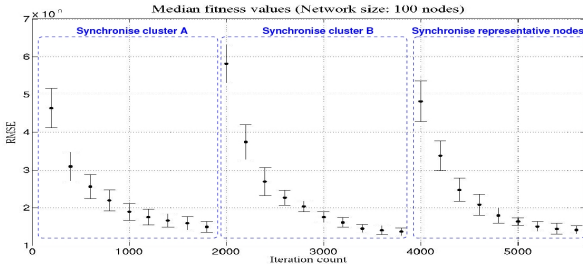
- $\zeta'_h = \Re \left(m(t) \text{RSS}_h e^{j2\pi f_c t (\gamma_h + \phi_h + \psi_h + \gamma_i - \gamma'_i)} \right)$

Ideal conditions: All nodes should now in phase

- 5 Final synchronisation among all nodes

Alternative algorithmic approaches

Hierarchical clustering



Alternative algorithmic approaches

Hierarchical clustering

Potential problem : Phase noise

- Only one cluster synchronised at a time
- Due to practical properties of oscillators, phases of nodes in the inactive clusters experience phase noise and start drifting out of phase
- Sufficient synchronisation possible in the order of milliseconds

Positive :

- No inter-node communication required

Open Issue :

- More than one hierarchy stage might be optimal
- for optimisation time
- for energy consumption
- Optimum hierarchy depth and cluster size derived by integer programming in time $\mathcal{O}(n^2)$

Alternative algorithmic approaches

Hierarchical clustering

Determine optimum cluster size and hierarchy depth :

- Expected optimisation time:

$$E[T_{\mathcal{P}_n}] = c \cdot k \cdot n \cdot \log(n)$$

- Expected energy consumption:

$$E[\mathcal{E}_{\mathcal{P}_n}] = c \cdot k \cdot n \cdot \log(n) \cdot \overline{\mathcal{E}_{\mathcal{P}_n}}$$

Hierarchy and cluster structure that minimises these formulae optimal

Alternative algorithmic approaches

Hierarchical clustering

Opt. cluster size and hierarchy depth (integer programming) :

- For a cluster size of m :

$$E[T_{\mathcal{P}_n}] = E[T_{\mathcal{P}_{\frac{n}{m}}}] \cdot \frac{n}{m} \cdot E[T_{\mathcal{P}_m}]$$

$$E[\mathcal{E}_{\mathcal{P}_n}] = E[\mathcal{E}_{\mathcal{P}_{\frac{n}{m}}}] \cdot \frac{n}{m} \cdot E[\mathcal{E}_{\mathcal{P}_m}].$$

- Define recursion by

$$E_{\text{opt}}[T_{\mathcal{P}_n}] = \min_m \left[E_{\text{opt}}[T_{\mathcal{P}_{\frac{n}{m}}}] \cdot \frac{n}{m} \cdot E_{\text{opt}}[T_{\mathcal{P}_m}] \right]$$

$$E_{\text{opt}}[\mathcal{E}_{\mathcal{P}_n}] = \min_m \left[E_{\text{opt}}[\mathcal{E}_{\mathcal{P}_{\frac{n}{m}}}] \cdot \frac{n}{m} \cdot E_{\text{opt}}[\mathcal{E}_{\mathcal{P}_m}] \right]$$

- Start of recursion (η min feasible cluster size):
 - $E_{\text{opt}}[T_{\mathcal{P}_\eta}]$
 - $E_{\text{opt}}[\mathcal{E}_{\mathcal{P}_\eta}]$

Alternative algorithmic approaches

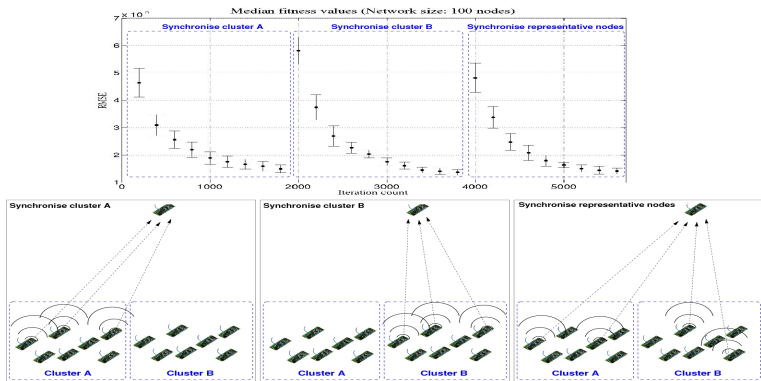
Hierarchical clustering

Opt. cluster size and hierarchy depth (integer programming) :

- Time required for calculation is quadratic.
 - With a network of n nodes, at most n^2 distinct terms
 - $E_{\text{opt}}[T_{\mathcal{P}_i}]$
 - $E_{\text{opt}}[\mathcal{E}_{\mathcal{P}_i}]$
- Start calculation at
 - $E_{\text{opt}}[\mathcal{E}_{\mathcal{P}_\eta}]$
 - $E_{\text{opt}}[T_{\mathcal{P}_\eta}]$
- All other values by table loop-up in time $\mathcal{O}(n^2)$ according to
 - $E_{\text{opt}}[T_{\mathcal{P}_n}]$
 - $E_{\text{opt}}[\mathcal{E}_{\mathcal{P}_n}]$ in time $\mathcal{O}(n^2)$

Alternative algorithmic approaches

Hierarchical clustering



- Reduction of synchronisation time and transmission power
- Calculation of optimum cluster size and depth in $\mathcal{O}(n^2)$

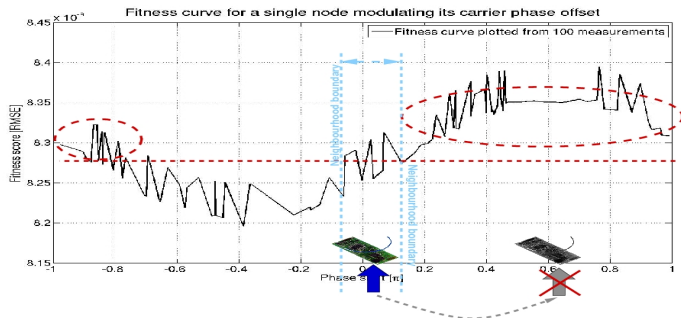
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Scenario analysis and algorithmic improvement

Local random search



- Global random search:
 - Synchronisation performance might deteriorate when the optimum is near
- With small local search space:
 - Majority of worse points excluded

Local random search

An upper bound on the synchronisation performance

Assumptions :

Mutation probability: n^{-1}

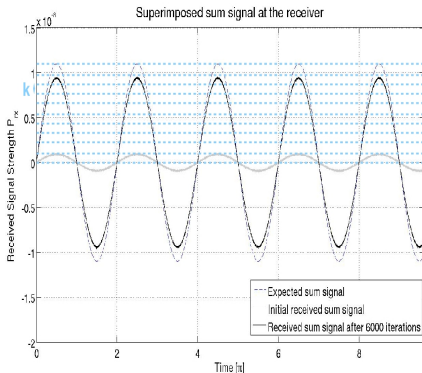
Uniform phase alteration

Initial distance to the optimum :

$$\geq \frac{n \cdot \log(k)}{2} \text{ (Chernoff)}$$

Technical assumption :

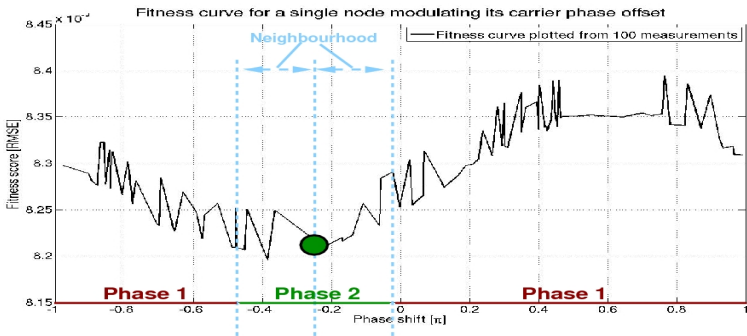
Fitness space divided in k slices of identical width



Local random search

An upper bound on the synchronisation performance

Analysis in two phases for the synchronisation process



Phase 1: Optimum outside search neighbourhood for at least one node

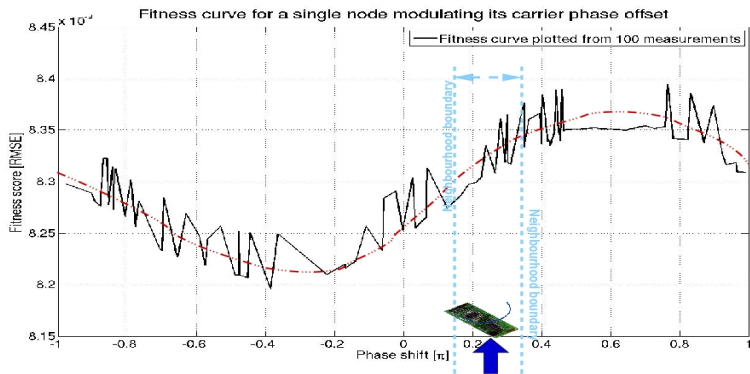
Phase 2: Optimum within search neighbourhood for all nodes

Local random search

An upper bound on the synchronisation performance

Phase 1: Optimum is outside the neighbourhood

- Reach search point with improved fitness: $\geq \frac{1}{2}$



Local random search

An upper bound on the synchronisation performance

When i signals synchronised:

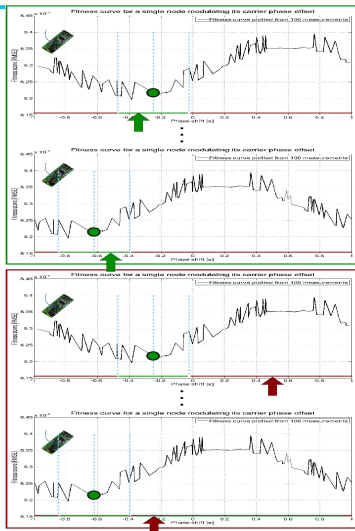
- Improve $n - i$ non-optimal signals
- i already optimal ones unchanged:

$$(n - i) \cdot \frac{1}{n} \cdot \frac{1}{2} \cdot \left(1 - \frac{1}{n}\right)^i \\ = \frac{n-i}{2n} \cdot \left(1 - \frac{1}{n}\right)^i$$

- since $\left(1 - \frac{1}{n}\right)^n < e < \left(1 - \frac{1}{n}\right)^{n-1}$

$$s_i \geq \frac{n-i}{2en}$$

- Expected number of mutations to increase fitness bounded by s_i^{-1} .

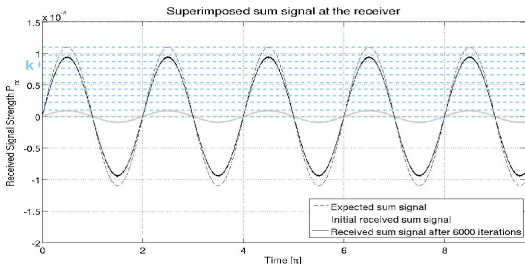


$n-i$

Local random search

An upper bound on the synchronisation performance

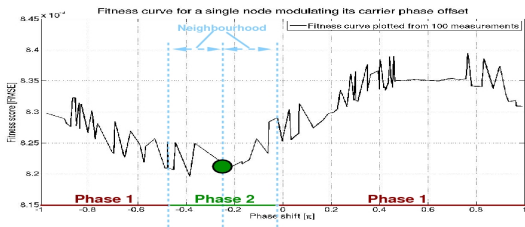
- Time until optimum is within the neighbourhood?
 - Constant time to leave slice
 - k distinct slices



$$\begin{aligned} E[T_P] &\leq c \cdot \sum_{i=0}^k \frac{2en}{n-i} = 2cen \cdot \sum_{i=1}^{k+1} i^{-1} \\ &< 2cen \cdot \ln(k+1) = \mathcal{O}(n \cdot \log(k)) \end{aligned}$$

Local random search

An upper bound on the synchronisation performance



Phase 2: Optimum within search neighbourhood

- Worst case: Increase fitness with probability $\frac{1}{N}$
- Similar to consideration above:

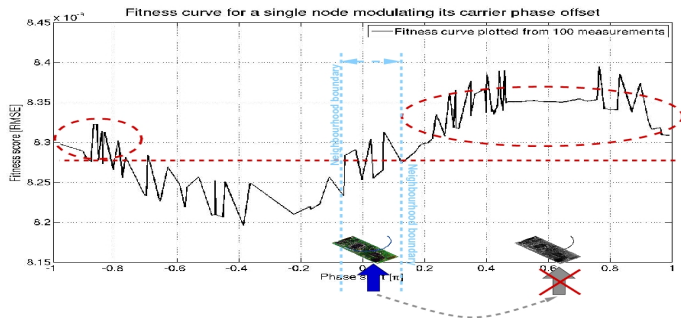
$$\mathcal{O}(N \cdot n \cdot \log(k))$$

Overall synchronisation time :

$$\mathcal{O}(N \cdot n \cdot \log(k)).$$

Scenario analysis and algorithmic improvement

Local random search



A lower bound on the synchronisation time :

- Method of the expected progress
- Similar to estimation for global random search
- Basically: Substitute network size n by neighbourhood size N

Scenario analysis and algorithmic improvement

Local random search

A lower bound on the synchronisation time :

- Method of the expected progress
- Similar to estimation for global random search
- Basically: Substitute network size n by neighbourhood size N
 - Probability to alter individual bit

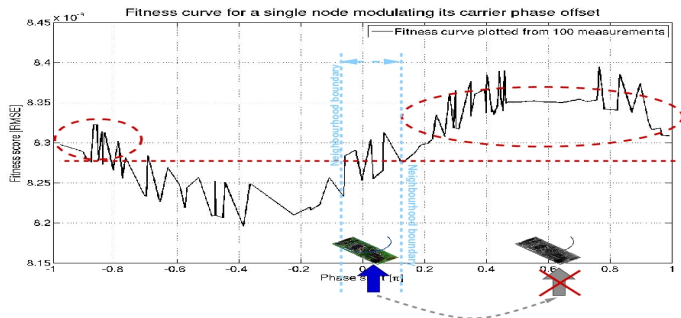
$$\frac{1}{N \cdot \log(k)}$$

- Instead of

$$\frac{1}{n \cdot \log(k)}$$

Scenario analysis and algorithmic improvement

Local random search



A lower bound on the synchronisation time :

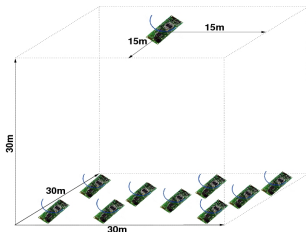
- With similar arguments as for global random search, lower bound

$$\Omega(N \cdot \log(k) \cdot \Delta)$$

Mathematical simulation environment

Impact of the node choice

Property	Value
Node distribution area	30m × 30m
Location of the receiver	(15m, 15m, 30m)
Mobility	stationary nodes
Base band frequency	$f_{base} = 2.4 \text{ GHz}$
Transmission power of nodes	$P_{tX} = 1 \text{ mW}$
Gain of the transmit antenna	$G_{tX} = 0 \text{ dB}$
Gain of the receive antenna	$G_{rX} = 0 \text{ dB}$
Iterations per simulations	6000
Identical simulation runs	10
Random noise power [46]	-103 dBm
Pathloss calculation (P_{rX})	$P_{tX} \left(\frac{\lambda}{2\pi d} \right)^2 G_{tX} G_{rX}$

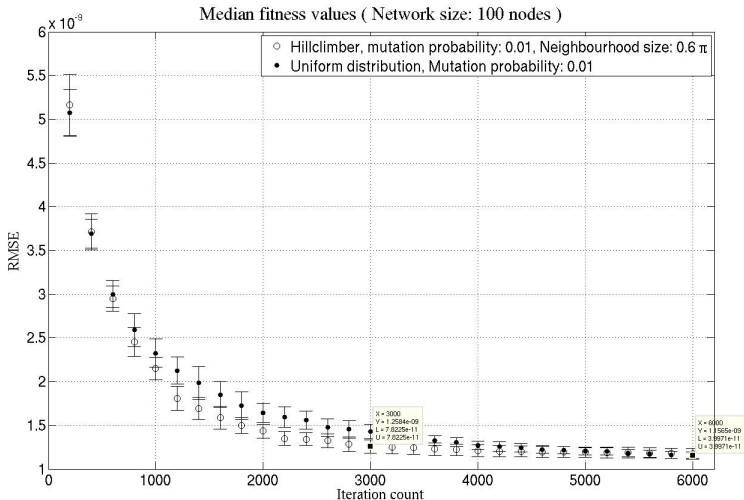


- Fitness measure:

$$RMSE = \sqrt{\sum_{t=0}^{\tau} \frac{(\sum_{i=1}^n S_i + S_{noise}(i) - s^*)^2}{n}}$$

Scenario analysis and algorithmic improvement

Local random search



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Multivariable equations

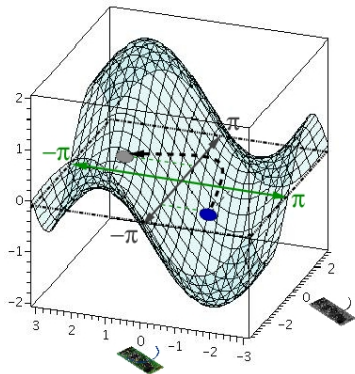
Received sum signal

- Reduce the amount of randomness in the optimisation
- Improve the synchronisation performance
- Improve the synchronisation quality

Scenario analysis and algorithmic improvements

Search space

- Search space:
 - Spanned by all Configurations of carrier phase offsets γ_i
- Search point / Configuration:
 - One possible configuration of carrier phase offsets

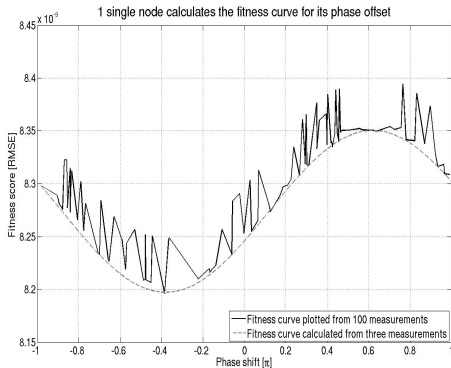


Multivariable equations

Received sum signal

- Fitness function observed by single node
- Constant carrier phase offset for $n - 1$ nodes
- Fitness function:

$$\mathcal{F}(\Phi_i) = A \sin(\Phi_i + \phi) + c$$

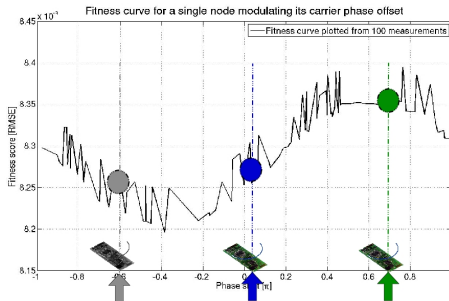


Multivariable equations

Received sum signal

Approach:

- Measure feedback at 3 points
- Solve multivariable equations
- Apply optimum phase offset calculated

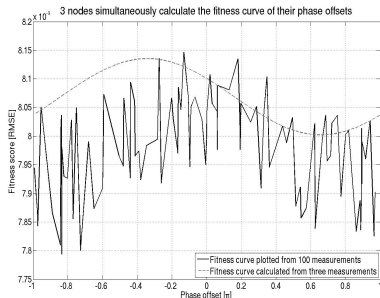
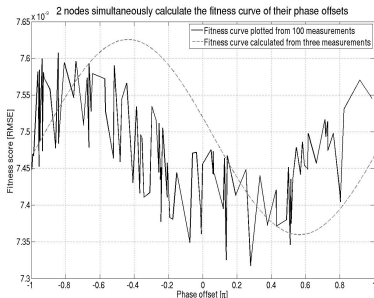


$$\mathcal{F}(\Phi_i) = A \sin(\Phi_i + \phi) + c$$

Multivariable equations

Received sum signal

- Problem:
 - Calculation not accurate when two or more nodes alter the phase of their transmit signals



Multivariable equations

Solution

An active node will :

- 1 Transmit with three distinct phase offsets $\gamma_1 \neq \gamma_2 \neq \gamma_3$ and measure feedback.
- 2 From these three feedback values and phase offsets, estimate feedback function and optimum phase offset γ_i^* .
- 3 Transmit a fourth time with $\gamma_4 = \gamma_i^*$.
- 4 If the deviation is less than 1% save γ_i^* as optimal phase offset, otherwise discard it.

A passive node will :

- 1 Transmit 4 times with identical phase offset γ_i .

Multivariable equations

Solution

- Node estimates the quality of the function estimation itself
- Transmit with optimum phase offset and measure channel again
- When Expected fitness deviates significantly from measured fitness, discard altered phase offset
- Deviation:
 - 1 node: $\approx 0.6\%$
 - 2 nodes: $\approx 1.5\%$
 - 3 nodes: $> 3\%$



Multivariable equations

Synchronisation process



- 1 Transmit with phase offsets $\gamma_1 \neq \gamma_2 \neq \gamma_3$; measure feedback
- 2 Estimate feedback function and calculate γ_i^*
- 3 Transmit with $\gamma_4 = \gamma_i^*$
- 4 If deviation smaller 1% finished, otherwise discard γ_i^*

Multivariable equations

Received sum signal

- Asymptotic synchronisation time:

$$\mathcal{O}(n)$$

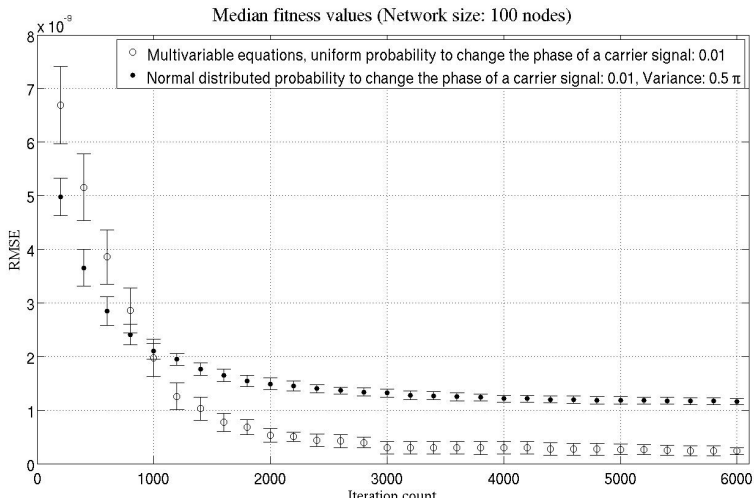
- Classic approach:¹

$$\Theta(n \cdot k \cdot \log(n))$$

¹Sigg, El Masri and Beigl, A sharp asymptotic bound for feedback based closed-loop distributed adaptive beamforming in wireless sensor networks (submitted to Transactions on Mobile Computing)

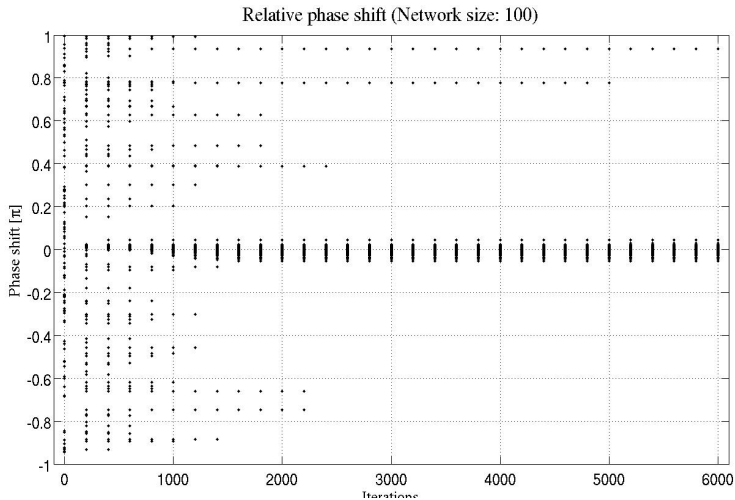
Multivariable equations

Performance estimation



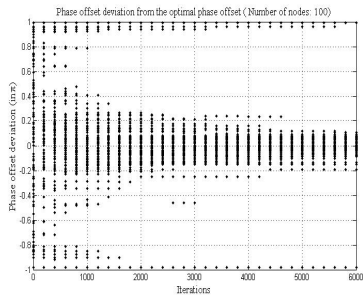
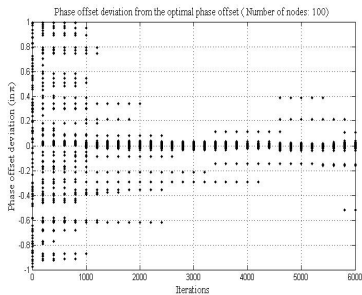
Multivariable equations

Performance estimation



Multivariable equations

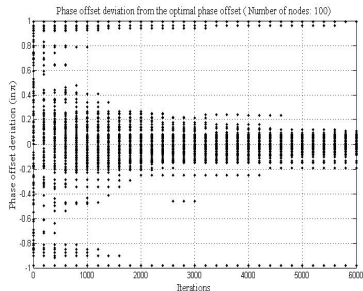
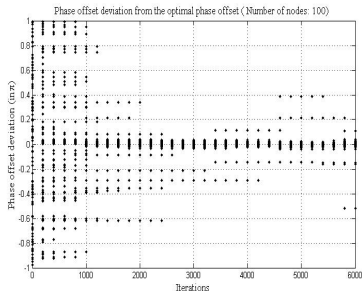
Performance estimation



- Phase offset of distinct nodes is within $+/- 0.05\pi$ for up to 99% of all nodes.

Multivariable equations

Performance estimation



- Asymptotically optimal synchronisation time
- Simulations: $\approx 12n$
- Further improvement:
 - 3 iterations per turn
 - Utilise last transmission from previous iteration

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Environmental changes

Introduction

- Velocity of nodes
- Multiple receiver nodes
- Increased population size
- Receive beamforming

Environmental changes

Velocity of nodes

Moving receiver :

- Straight line
- Random walk

Moving transmitter :

Straight line

Random walk

Environmental changes

Velocity of nodes

Moving receiver :

- Straight line
- Random walk

Aspects :

Only one moving node

Simple case

Also applicable when all transmitters move identically

Environmental changes

Velocity of nodes

Moving transmit nodes :

- Straight line
- Random walk

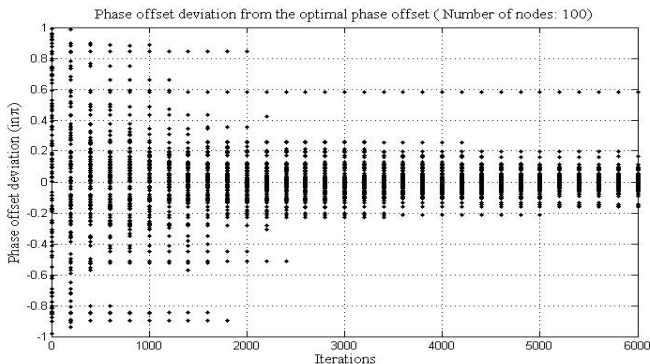
Aspects :

Multiple nodes moving

Hard case

Environmental changes

Velocity of nodes

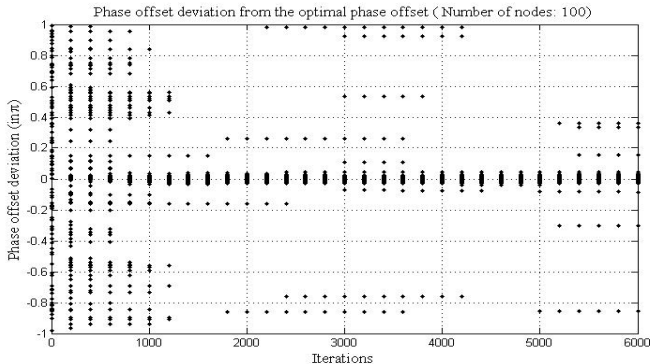


Random walk – receiver :

- Maximum velocity for classic algorithm: 5m/sec

Environmental changes

Velocity of nodes

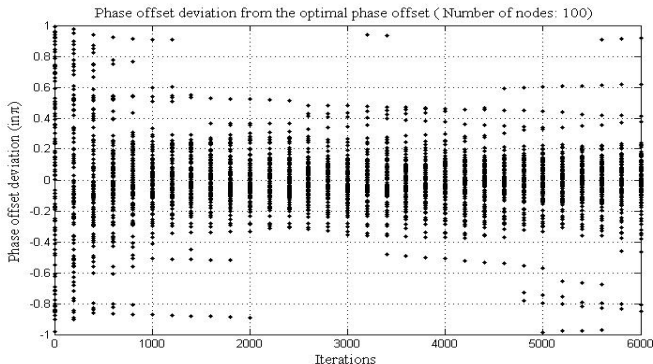


Random walk – receiver :

- Max. velocity for Multivariable equations:
5m/sec easily supported

Environmental changes

Velocity of nodes

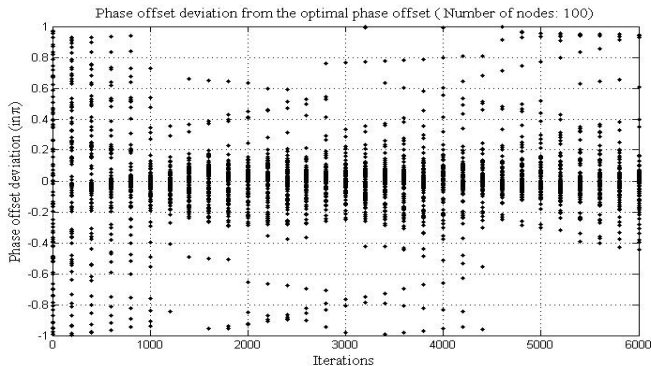


Random walk – transmitter :

- Maximum velocity for classic algorithm: 2m/sec

Environmental changes

Velocity of nodes

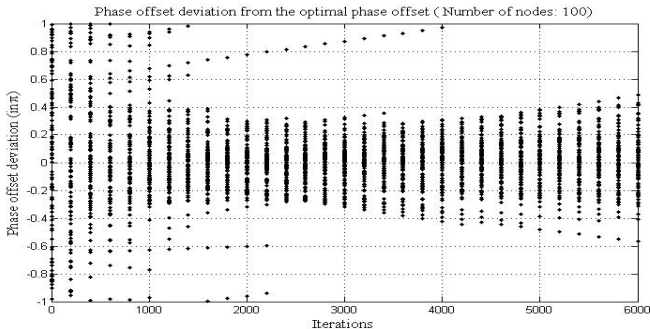


Random walk – transmitter :

- Max. velocity for Multivariable equations:
5m/sec supported

Environmental changes

Velocity of nodes

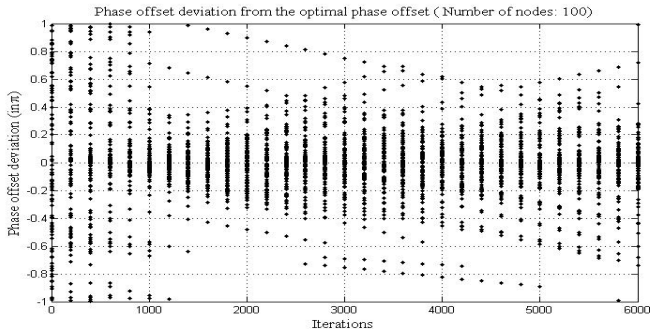


straight line – maximum relative speed :

- Maximum velocity for classic algorithm: 30m/sec
- Regardless if transmitter or receiver move

Environmental changes

Velocity of nodes



straight line – maximum relative speed :

- Maximum velocity for Multivariable equations algorithm: 60m/sec
- Regardless if transmitter or receiver move

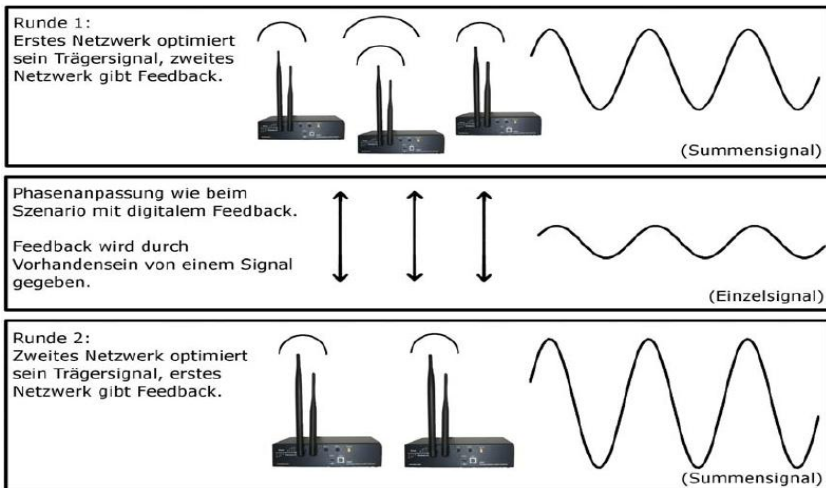
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Environmental changes

Multiple receiver nodes



Environmental changes

Multiple receiver nodes

3m

Knoten	<i>n0</i>	<i>n1</i>	<i>n2</i>	<i>m0</i>	<i>m1</i>
Gain zur Anfangsamplitude (Median) [dB]	0,96	2,39	1,40	1,46	1,10
Gain zu einem Knoten (Median) [dB]	2,33	2,32	2,37	3,50	4,05
Anzahl letztes Feedback	5/11	3/11	3/11	8/11	7/11
Amplitude nach Synchronisation [%]	92,4	51,4	65,3	91,0	90,7

12m

Knoten	<i>n0</i>	<i>n1</i>	<i>n2</i>	<i>m0</i>	<i>m1</i>
Gain zur Anfangsamplitude (Median) [dB]	1,24	0,63	1,39	2,06	1,47
Gain zu einem Knoten (Median) [dB]	2,53	1,09	2,00	2,74	4,18
Anzahl letztes Feedback	2/10	4/10	4/10	5/10	5/10
Amplitude nach Synchronisation [%]	57,1	92,0	86,5	86,4	86,6

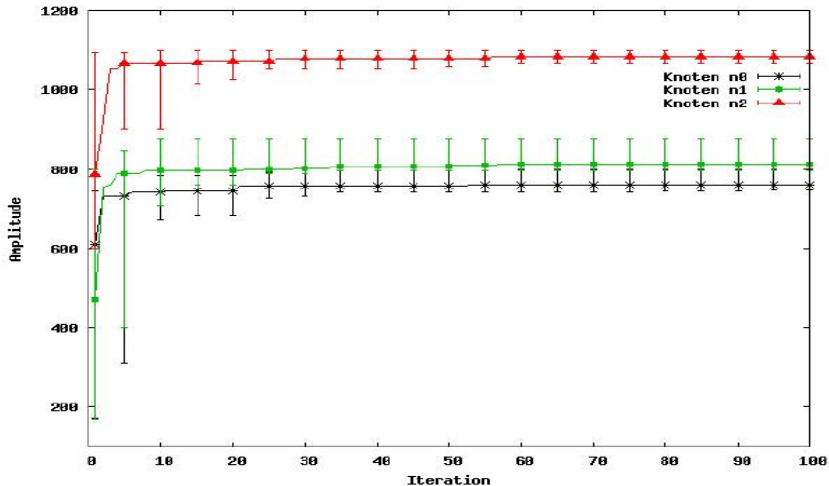
24m

Knoten	<i>n0</i>	<i>n1</i>	<i>n2</i>	<i>m0</i>	<i>m1</i>
Gain zur Anfangsamplitude (Median) [dB]	1,12	2,33	2,76	3,61	1,67
Gain zu einem Knoten (Median) [dB]	1,2	2,54	2,03	5,15	3,76
Anzahl letztes Feedback	4/5	0/5	1/5	4/5	3/5
Amplitude nach Synchronisation [%]	94,2	80,0	61,4	95,8	97,9

Environmental changes

Multiple receiver nodes

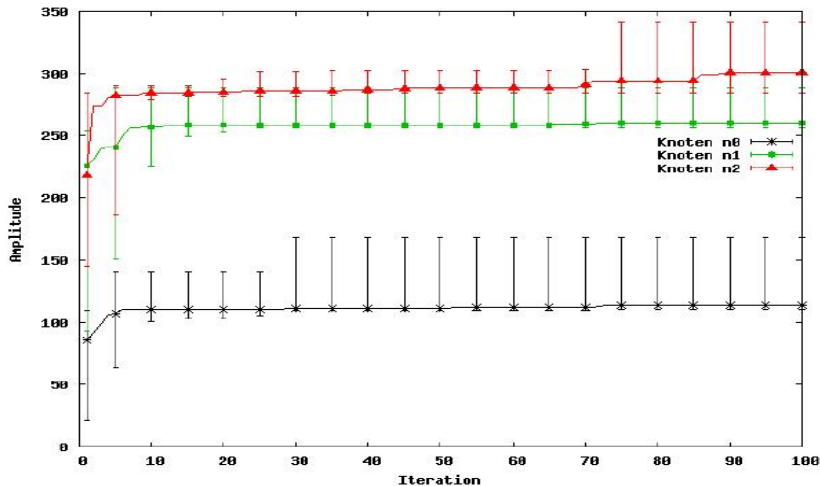
3m



Environmental changes

Multiple receiver nodes

12m



Environmental changes

Multiple receiver nodes

Multiple receiver nodes – issues :

- Only binary feedback value
 - Therefore only classic optimisation approach
- Distance between transmit and receive nodes relative to spatial diversity of nodes in one network
 - Better synchronisation when nodes in one network in spatial proximity
 - When nodes in one network communicate: No issue

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Environmental changes

Increased population size

Increased population size – Discussion :

How to achieve population size greater than one?

- Separate transmit times
- WCDMA
- Distinct frequencies simultaneously

Only separate transmit times feasible for WSN

More time for each iteration

- Initial solution: Random search
- Not clear if performance improvement possible by crossover

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Environmental changes

Receive beamforming

Receive beamforming – Discussion :

- Transmit node transmits only once
- Receiver nodes combine received signal fragments in the network
- Tradeoff:
 - Transmission power for in-network communication
 - Transmission over several iterations with receiver node
- More complex computation of transmit nodes

Questions?

- Introduction to context aware computing
- Wireless sensor networks
- Wireless communications
- Basics of probability theory
- Randomised search approaches
- Cooperative transmission schemes
- Distributed adaptive beamforming
 - Feedback based approaches
 - Asymptotic bounds on the synchronisation time
 - Alternative algorithmic approaches
 - Alternative Optimisation environments