# Algorithms for context prediction in Ubiquitous Systems

Exact sequence Matching

Stephan Sigg

Institute of Distributed and Ubiquitous Systems Technische Universität Braunschweig

November 18, 2008

Stephan Sigg

Algorithms for context prediction in Ubiquitous Systems

#### **Overview and Structure**

- Introduction to context aware computing
- Basics of probability theory
- Algorithms
  - Simple prediction approaches: ONISI and IPAM
  - Markov prediction approaches
  - The State predictor
  - Alignment prediction
  - Prediction with self organising maps
  - Stochastic prediction approaches: ARMA and Kalman filter
  - Alternative prediction approahces
    - Dempster shafer
    - Evolutionary algorithms
    - Neural networks
    - Simulated annealing

#### **Overview and Structure**

- Introduction to context aware computing
- Basics of probability theory
- Algorithms
  - Simple prediction approaches: ONISI and IPAM
  - Markov prediction approaches
  - The State predictor
  - Alignment prediction
  - Prediction with self organising maps
  - Stochastic prediction approaches: ARMA and Kalman filter
  - Alternative prediction approahces
    - Dempster shafer
    - Evolutionary algorithms
    - Neural networks
    - Simulated annealing

#### Outline Simple prediction approaches: ONISI and IPAM



Exact sequence matching





In Ubiquitous Computing

- Prediction accuracy
- High prediction horizon
- Adaptability
- Memory and processing load
- Multi-dimensional time series
- Iterative prediction
- Prediction of context durations
- Relaxation of typical behaviour patterns
- Context data types
- Pre-processing of time series data

Prediction accuracy

- Context prediction is an optimisation problem
  - Prediction errors have to be minimised
  - Low error probability desired

High prediction horizon

- A prediction algorithm shall provide a high prediction horizon
- At the same time: low error probability
- Prediction accuracy decreases with increasing prediction horizon
  - Low degradation speed desired

Adaptability

- Learning is essential in Ubiquitous Environments
  - Environment is subject to changes
    - typically slow changes
  - Behaviour patterns of persons might change due to external influences
    - Relocation
    - New Job
    - Vacancy
    - New semester and time schedule
- Without learning, prediction accuracy will decrease over time

Memory and processing load





- Devices for ubiquitous computing typically small scale and mobile
  - Low processing power
  - Restricted memory and storage size



- Typically several context sources attached to a device
- The time series observed is therefore multi-dimensional
- Algorithms that are only applicable to one-dimensional input unsuited in many scenarios
  - Solution: Model multi-dimensional TS by several one-dimensional TS
  - Problem: Inter-relation between time series not modelled

- Ideallised: Context data sources synchonised
  - Very unlikely



- Realistic scneario: No synchonisation between context sources
  - Context sources push information when specific events occur
  - Duty cycling (time differs between context sources)



- Question: Which context values for a given time interval?
  - Interpolation of context values?
  - Last value measured?



- Proposal/Idea: Context reasoning by DAG<sup>1</sup>
  - Design processing sequence that the algorithm shall follow/respect?
  - Designed for context reasoning Also applicable for context prediction
  - Problems: How to design this processing graph on-line and autonomously?



<sup>&</sup>lt;sup>1</sup>Bernd Niklas Klein, Sian Lun Lau, Andreas Pirali, Tino Löffler, Klaus David. *DAGR-DAG based context* reasoning: An architecture for context aware applications. In Proceedings of the eighth international workshop on applications and services in wireless networks, Kassel, Germany, pp. 20-25, 2008.

Algorithms for context prediction in Ubiquitous Systems

Iterative prediction

- Prediction horizon can be extended by iterative prediction
  - Utilise predicted contexts as input
- Problem: Less accurate
  - Predicted contexts more error prone than measured values

Prediction of context durations

- Context durations make a difference
  - Different duration of contexts might also indicate other situations/Contexts
  - It is more difficult to predict a context together with its occurence time instead of simply a context sequence
  - Duration can be modelled by repeatedly occurring contexts in a context sequence

Relaxation of typical behaviour patterns

- Exact pattern matching not suited in most ubiquitous scenarios
  - Behaviour patterns do not reoccur 'exactly' but approximately
  - E.g. the route and time to some location will differ slightly for several times the route is taken.
- Approximate matching is more difficult:
  - Where to draw the line?
  - When are two time series considered as approximately matching and when not
  - Inherently dependent on given scenario
  - Typically solved by heuristic approach/metric

Relaxation of typical behaviour patterns



Context data types

- Context can have various data types
  - Nominal
  - Ordinal
  - Hierarchical
  - Numerical
- In multi-dimensional time series also multi-type contexts possible
- Most algorithms can only process some of these data types
  - Not applicable in scenarios where other data types are measured

Context data types

Nominal contexts





Context data types





- >
- =



Context data types

#### Hierarchical contexts

- Sub-contexts and parent contexts
- Contexts might be contained in others



Context data types

- Numerical contexts
  - Real valued, integer valued contexts
  - Complex mathematical operations possible
  - Best suited for context processing

#### Context data types

Algorithm	Ordinal contexts	Nominal contexts	Hierarchical contexts	Numerical contexts
BN	+	+	+	+
SVM	-	-	-	+
KM	-	-	-	+
MM	+	+	+	+
NN	+	+	+	+
NNS	-	$(+)^{7}$	(+)	+
SOM	-	$(+)^{7}$	$(+)^{7}$	+
PM	+	+	+	+
AP	$(+)^{7}$	$(+)^{7}$	$(+)^{7}$	+
ARMA	-	-	-	+
Kalman filters	-	-	-	+

Pre-processing of time series data

- For context prediction, preprocessing of context data is often applied
  - Identify typical context patterns
  - Derive occurrence probability of contexts
  - Derive context transition probabilities
- Distinguish between on-line and off-line processing
- Problem: Increased processing load

	IPAM	ONISI	Markov	CRF
Numeric Contexts				
Non-numeric Contexts				
Complexity				
Learning ability				
Approximate matching				
Multi-dim. TS				
Discrete data				
Variable length patterns				
Multi-type TS				
Continuous data				
Pre-processing				
Context durations				
Continuous time				

	PCA	SPM	Align	SOM
Numeric Contexts				
Non-numeric Contexts				
Complexity				
Learning ability				
Approximate matching				
Multi-dim. TS				
Discrete data				
Variable length patterns				
Multi-type TS				
Continuous data				
Pre-processing				
Context durations				
Continuous time				

	ARMA	Kalman	SVM	DS
Numeric Contexts				
Non-numeric Contexts				
Complexity				
Learning ability				
Approximate matching				
Multi-dim. TS				
Discrete data				
Variable length patterns				
Multi-type TS				
Continuous data				
Pre-processing				
Context durations				
Continuous time				

		EAs	NN	Sim. Anneal
Num	eric Contexts			
Non-	numeric Contexts			
Com	plexity			
Lear	ning ability			
Appr	oximate matching			
Mult	i-dim. TS			
Disci	rete data			
Varia	ble length patterns			
Mult	i-type TS			
Cont	inuous data			
Pre-p	processing			
Cont	ext durations			
Cont	inuous time			

#### Outline Simple prediction approaches: ONISI and IPAM



Exact sequence matching





Stephan Sigg

Algorithms for context prediction in Ubiquitous Systems

#### Introduction

- File a given sequence for the exact occurence of a sub-sequence
- 'Pattern Matching' or 'String Matching'<sup>2</sup>
- Easily extended to context prediction:
  - Prediction  $\equiv$  continuation of matched sequence



<sup>&</sup>lt;sup>2</sup>Richard O. Duda, Peter E. Hard and David G. Stork, *Pattern Classification*, Wiley-Interscience, 2nd edition, 2001.

Notation

#### Strings and patterns

A string is a sequence of letters such as 'AGCTTCGAATC'. Context patterns can be represented as strings when each context is assigned a letter.



#### Substring

Any contiguous string that is part of another string is called a substring. For example, 'GCT' is a substring of 'AGCTTC'.

Stephan Sigg

Algorithms for context prediction in Ubiquitous Systems

Notation

#### String matching

Given two Strings  $\mathbf{x}$  and  $\mathbf{y}$ , string matching is the problem to determine whether  $\mathbf{x}$  is a substring of  $\mathbf{y}$  and, if so, where it appears.

#### Edit distance

Given two strings x and y, the edit distance describes the minimum number of basic operations – character insertions, deletions and exchanges – needed to transform x into y.

Example

Suppose we have a large text such as Herman Melville's Moby Dick and want to classify it as relevant to the topic of fish or to the topic of hunting.

- Keywords for the fish topic
  - might include 'salman', 'whale', fishing', 'ocean'
- Keywords for hunting
  - might include 'gun', 'bullet', 'shoot'.
- String matching would determine the number of occurrences of such keywords in the text.
- A simple count of keyword occurrences could then be used to classify the text according to topic

String matching

#### Task

Determine whether a candidate string  $\mathbf{x}$  is a substring of  $\mathbf{y}$ .

• Typically:  $\mathbf{x} \ll \mathbf{y}$ 

 $\bullet\,$  Each character in x and y is taken from an alphabet  $\Sigma\,$ 

- DNA bases,
- Binary sequences  $(\Sigma = \{0, 1\})$
- Alphanumeric sequences (Σ = {0, ..., 9, a, ..., z, A, ..., Z})
- Context sequences Each character represents a context

String matching

#### Basic string matching problem

For two strings x and y, determine whether a shift s at which the string x is perfectly matching with each caracter of y beginning at position s + 1.


String matching

Straightforward approach

Subsequently test each possible shift s

#### Example

String matching

- The straightforward algorithm is, however, far from optimal
- Worst case runtime:

•  $\Theta((n-m+1)m)$ 

• Problem: Information known from one candidate shift *s* is not exploited for the subsequent candidate shift

String matching

```
Boyer-Moore string matching
1 begin initialise \Sigma x,y,n=length[y], m=length[x]
2
       F(\mathbf{x}) \leftarrow last-occurrence function
3
       G(\mathbf{x}) \leftarrow good-suffic function
4
       s \leftarrow 0
5
       while s \leq n - m
6
           do i \leftarrow m
7
           while j > 0 and x[j] = y[s + j]
8
               do i \leftarrow i - 1
9
           if i = 0
10
                then print 'pattern occurs at shift' s
11
                    s \leftarrow s + G(0)
12
                else s \leftarrow s + max[G(i), i - F(y[s + i])]
13
         return
14 end
```

Boyer-Moore string matching algorithm

- The Boyer-Moore algorithm utilises information known from recent candidate shifts
- Character compositions are done in reverse order
- increment to a new shift need not be 1
- Benefits from two heuristics:
  - Good suffix heuristic
  - Bad character heuristic

Bad character heuristic and good suffix heuristic



Algorithms for context prediction in Ubiquitous Systems

Bad character heuristic and good suffix heuristic

- Bad character heuristic
  - Since character comparisons proceed from right to left, bad character is found as efficiently as possible
  - Since current shift *s* is invalid, no additional character comparisons are required
  - Proposes incrementing the shift by an amount to align the rightmost occurrence of the bad character in **x** with the bad character identified in **y**.
  - No valid shifts have been dropped
- Good suffix heuristic
  - A suffix of **x** is a substring of **x** that contains the final character in **x**
  - At shift *s* the rightmost contiguous characters in **y** that match those in **x** are called the good suffix
  - Character comparisons are made from right to left and are therefore optimal

Algorithms for context prediction in Ubiquitous Systems

#### Last occurrence function

- Table containing every letter in the alphabet
- Plus position of its rightmost occurrence in x
- Example:
  - A, 4
  - B, 5
  - C, 3
- Computation only once
  - Does not significantly impact the runtime



Good suffix function

- Creates table that for each suffix gives location of second right-most occurrence in **x**
- Example:
  - B, 2
  - AB, 1
  - CAB, -
  - BCAB, -
  - ABCAB, -
- Computation only once
  - Does not significantly impact the runtime



Boyer-Moore algorithm

- Computational complexity
  - Homework / Exercise ;-)

Asymptotic computation time

 $O(k) \mapsto computation time not larger than <math>c \cdot k$  for a suitable constant c and k large.

Problems

Problems with exact string matching approaches in Ubiquitous Computing

- Data might be distorted by noise
  - In Ubicomp scenarios we even expect noisy input data
  - Exact pattern matching not feasible then

Approximate matching approaches

- Edit distance
- Nearest neighbour approaches

Approximate matching approaches

- Nearest neighbour approaches
  - Strings are identified as vectors in a coordinate system
  - Since these vectors are numerical, distance/similarity between vectors can be computed by common metrics
- We will consider these approaches later in the lecture

Approximate matching approaches

- Edit distance
  - Task: Compute the difference
  - Problem: What is the similarity/distance between string sequences?
  - Example: is 'abbccc' closer to 'aabbcc' or to 'abbcccb'?
- We will consider these approaches later in the lecture

#### Outline Simple prediction approaches: ONISI and IPAM



Exact sequence matching





Stephan Sigg

Algorithms for context prediction in Ubiquitous Systems

Introduction and scenario

#### Scenario

Predict the next command in a series of command line inputs to a UNIX shell

#### Prediction of next command on a UNIX shell<sup>a</sup>

. . . 96102513:34:49 cd 96102513:34:49 ls 96102513:34:49 emacs 96102513:34:49 exit 96102513:35:32 BLANK 96102513:35:32 cd 96102513:35:32 cd 96102513:35:32 rlogin 96102513:35:32 exit 96102514:25:46 BLANK 96102514:25:46 cd 96102514:25:46 telnet 96102514:25:46 ps 96102514:25:46 kill 96102514:25:46 emasc 96102514:25:46 emacs 96102514:25:46 cp 96102514:25:46 emacs

<sup>&</sup>lt;sup>a</sup>B.D. Davison and H. Hirsh, *Predicting* sequences of user actions. In: AAAI/ICML Workshop on predicting the future: AI approaches to time-series analysis. 1998

Introduction and scenario

- It was observed that recently issued commands had the greatest impact on the follow-up command
- Idea: Standard learning algorithms ignore rare but possibly important events in a time series
  - IPAM was designed to improve this

#### Example

Predict hardware failures in routing networks. Typically every packet is routed as expected and no error occurs. In some, very rare cases, a hardware router might collapse. Likely result: packet losses, congestion, re-calculation of routing tables or a disconnected part of the network.

The event is rare but serious.

Introduction and scenario

- Requirements of an optimal on-line learning algorithm
  - Have predictive accuracy at least as good as the bset known resource-unlimited methods
  - Operate incrementally (Modifying existing model rather than building a new one as new data is optained)
  - Be affected by all events (remembering uncommmon, but useful, events regardless of how much time has passed)
  - Do not necessarily retain a copy of all events observed
  - Output a list of predictions sorted by confidence
  - Adapt to changes to the target concept
  - Be fast enough for interactive use
  - Learn by passive observation
  - Apply even by absence of domain knowledge

Algorithmic approach

- IPAM (Incremental Probabilistic Action Modeling)
  - on-line learning algorithm
  - Utilises last few events issued in order to predict the next event in a sequence of events
  - Prediction horizon: 1
  - Interative prediction possible
  - Impact of empiric factor:  $\alpha$

Algorithmic approach

- Algorithmic operation
  - While observing sequence: matrix of prediction probabilities is maintained.
  - Colums: all possible events,
  - Rows: added and modified as events occur.
  - First event c<sub>i</sub>: New row is added
    - Each column in this row holds probability that event observed after *c<sub>i</sub>* was observed.
  - Row initialised with uniform probabilities  $\frac{1}{n}$
  - Next event  $c_{i+1}$ : New row added and initialised with uniform probabilities.
  - Preceding row, every column multiplied with  $0 \le \alpha \le 1$  and column  $c_i$  increased by  $(1 \alpha)$ .
  - Probability to predict event sequences that have not been observed for some time diminishes

Algorithmic approach - operation principle



 Step 2:

  $c_i$   $c_i$   $c_{i+1}$   $\cdots$ 
 $c_i$   $\frac{1}{n}$   $\frac{1}{n}$   $\frac{1}{n}$ 
 $c_i$   $\frac{1}{n}$   $\frac{1}{n}$   $\frac{1}{n}$ 

Step 3:

			-		
	•••	Ci		$c_{i+1}$	
Ci		$\frac{1}{n} \cdot \alpha + (1 - \alpha)$	$\frac{1}{n} \cdot \alpha$	$\frac{1}{n} \cdot \alpha$	
c <sub>i+1</sub>		$\frac{1}{n}$	$\frac{1}{n}$	$\frac{1}{n}$	

Results and figures

- Collected command histories of 77 users (mostly undergraduate students)
- Over 168,000 commands executed
- During a period of 2-6 months
- Average user over 2000 command instances
- 77 distinct commands per user on average
- 8.4% of the commands were new and had not been logged previously
- Users repeated the last command 20% of the time

Results and figures



Results and figures



Prediction accuracy



Adaptability

- The IPAM algorithm has only restricted ability to adapt to changing environments
  - It can learn new context sequences
  - The importance of the occurrence of context sequences can change
  - No support for newly observed contexts
  - When new contexts occur in an environment, the algorithm can not make use of this

Memory and processing load

- Memory load
  - IPAM keeps a table in memory of size  $O(k^2)$
  - k = number of distinct commands
- Processing load
  - Predictions performed in constant time
  - Updates require time O(k)

Multi-dimensional time series

- The IPAM algorithm is not well suited for multi-dimensional time series
  - It was designed for one-dimensional command-line input
  - In scenarios with more than one context source the approach is not feasible
  - Possible: Aggregation of multi-dimensional time series to one-dimensional time series.

Iterative prediction

#### • Iterative Prediction possible

• Steep decrease in prediction accuracy expected since prediction horizon is only 1

Prediction of context durations

- Prediction of context duration not possible
  - Algorithm was designed to predict the occurrence of the next event.
  - Event durations are not considered by the algorithm
  - Only simple sequence of occurring events possible

Approximate matching of patterns

#### Exact pattern matching

- The IPAM algorithm utilises exact pattern matching
- Approximate matching was not implemented
- Theoretically it is possible to implement approximate matching for the IPAM algorithm.

Context data types

- All data types supported by IPAM
  - Cathegorical data utilised for prediction
  - IPAM considers typical context patterns for prediction
  - Numerical, fluctuating data will, however blow up the memory requirement and decrease the prediction accuracy as exact pattern matching is applied.
  - Trends are not considered

Pre-processing

- Pre-processing required but low computational complexity
- Algorithm designer has to specify all possible events/contexts
- Computational complexity to initialise the prediction matrix: O(k)

Conclusion

- Low computational complexity
- Low memory requirements
- Cathegorical time series prediction
- Prediction of typical patterns no trends considered
- Prediction history only of length 2 Complex command sequences can thus not be distinguished
- All events known in advance: No adaptive operation when also occuring contexts might change.
- Not well suited for flexible, changing ubiquitous environments

### Aspects of prediction algorithms

Summary

	IPAM	ONISI	Markov	CRF
Numeric Contexts	yes			
Non-numeric Contexts	yes			
Complexity	O(k)			
Learning ability	(no)			
Approximate matching	no			
Multi-dim. TS	(no)			
Discrete data	yes			
Variable length patterns	no			
Multi-type TS	yes			
Continuous data	no			
Pre-processing	O(k)			
Context durations	no			
Continuous time	no			

#### Outline Simple prediction approaches: ONISI and IPAM



- Exact sequence matching
- 3 Algorithm: IPAM
- 4 Algorithm: ONISI

# Algorithm: ONISI

Introduction and scenario

#### Scenario

The use of an unmodified application by a user shall be observed in order to build application and usage-models

- Observe user-interactions with the application interface<sup>3</sup>
- From these observations a state-space is build which the user navigates
- Stochastic properties of state transitions are also modelled
- Task: Observe a user and model its decision process

<sup>&</sup>lt;sup>3</sup>Peter Gorniak and David Poole, *Predicting future user actions by observing unmodified applications*. In Proceedings of the Seventeenth National Conference on Artificial Intelligence and Twelfth Conference on Innovative Applications of Artificial Intelligence, pp. 217-222, 2000.

Algorithms for context prediction in Ubiquitous Systems
Introduction and scenario

- Challenges when recent results are to be applied to new application
  - Results often do not transfer easily
  - Implementation used in research uses modified application
    - Non-trivial to repeat modification
    - Time-consuming to repeat modification
    - increases application complexity.
  - Hand-crafted application models required
    - time consuming

Introduction and scenario

#### Approach

Extract knowledge from a user's interaction with the application

- No prior knowledge of the application
  - Purpose
  - Structure
- No modification to the application
- Predict future actions building on the usage-model extracted from an application

Algorithmic approach

- ONISI (ON-line Implicit State Identification)
  - Assign probabilities to all possible actions in the currently observed interface state
  - Employs k nearest neighbours scheme
    - Metric: sequence match length
  - Java implementation
    - Wrapper to existing java applications
    - Able to record interfaces of java applications
    - No modification of application required

Algorithmic approach

#### State of a user

A state of a user consists of a combination of the user's internal state and the application's interface state.

• Attempt: Try to determine the policy the user is employing from our observation of the user's interaction history.

Algorithmic approach

- Prediction: Search interaction history for behavioural patterns similar to current pattern
- Required:
  - Observed pattern to extract from the interaction history
  - Method to determine occurrence of pattern in history
  - Function that ranks possible actions

Algorithmic approach – Extraction of observed pattern

#### • Length of patterns automatically varied

- Longer patterns are deemed more important
- Patterns are chosen to be longest sequences in histroy that match immediate history

Measure 1: Length

Sequences that prediction action a are computed by  $I_t(s, a)$ 

Average of lenghts of k longest sequences that end with action a in state s and match history sequence immediately prior to time t

- Possible actions are ranked according to  $l_t(s, a)$
- $\frac{l_t(s,a)}{\sum_i l_t(s,a_i)}$

Stephan Sigg

Algorithms for context prediction in Ubiquitous Systems

Algorithmic approach – Extraction of observed pattern

- Length of patterns automatically varied
  - More frequent patterns are deemed more important

Measure 2: Frequency

Sequences that prediction action a are computed by  $f_t(s, a)$ 

Frequency at which a sequence is observed in history

- Possible actions are ranked according to  $f_t(s, a)$
- $\frac{l_t(s,a)}{\sum_i l_t(s,a_i)}$

Algorithmic operation

- Compare immediate history with state-action pair (s, a)
  - Running backwards through recorded history
  - Find k longest sequences that match immediate history
- Average length of sequences:  $I_t(s, a)$
- Count number of times a has occurred:  $f_t(s, a)$
- Return ranking

$$R_t(s,a) = \alpha \frac{l_t(s,a)}{\sum_i l_t(s,a_i)} + (1-\alpha) \frac{f(s,a)}{\sum_i f(s,a_i)}$$
(1)

Algorithmic operation



Assume:

α = 0.9

- All actions provide a sum  $\sum_{i} l_t(s, a) = 5$
- $a_3$  has occured 50 times,  $s_3$  has been visited 100 times

• Set of maximum length sequences: {2,1,0}

0

$$l_t(s_3, a_3) = \frac{0+1+2}{3} = 1$$
 (2)

۲

$$R_t(s_3, a_3) = 0.9\frac{1}{5} + 0.1\frac{50}{100} = 0.18 + 0.05 = 0.23 \quad (3)$$

Stephan Sigg

Algorithms for context prediction in Ubiquitous Systems

81/94

Results and figures - Performance at various parameter settings



Prediction accuracy - Performance



Prediction horizon

- Prediction horizon can be extended by iterative prediction
  - Utilise predicted contexts as input
- Problem: Less accurate
  - Predicted contexts more error prone than measured values

Adaptability

#### • The ONISI is well adaptable to arbitrary java applications

- It can learn new context sequences
- Also, new events can be observed

Memory and processing load

• Exercise ;-)

Stephan Sigg

Algorithms for context prediction in Ubiquitous Systems

Multi-dimensional time series

- The ONISI algorithm is not suited for multi-dimensional time series
  - It was designed for one-dimensional nput
  - In scenarios with more than one context source the approach is not feasible
  - Possible: Aggregation of multi-dimensional time series to one-dimensional time series.

Iterative prediction

#### • Iterative Prediction possible

• Steep decrease in prediction accuracy expected since prediction horizon is only 1

Prediction of context durations

- Prediction of context duration not possible
  - Algorithm was designed to predict the occurrence of the next event.
  - Event durations are not considered by the algorithm
  - Only simple sequence of occurring events possible

Approximate matching of patterns

#### Exact pattern matching

- The ONISI algorithm utilises exact pattern matching
- Approximate matching was not implemented
- Theoretically it is possible to implement approximate matching for the algorithm.

Context data types

Only cathegorical time series data supported by ONISI
ONISI considers typical context patterns for prediction

Pre-processing

- No Pre-processing required
- On-line approach

Conclusion

- Low computational complexity (?)
- Cathegorical time series prediction
- Prediction of typical patterns
- Prediction history or arbitrary length
- Frequency and length of patterns considered
- Not well suited for flexible, changing ubiquitous environments

#### Aspects of prediction algorithms

Summary

	IPAM	ONISI	Markov	CRF
Numeric Contexts	yes	no		
Non-numeric Contexts	yes	yes		
Complexity	O(k)	()		
Learning ability	(no)	yes		
Approximate matching	no	no		
Multi-dim. TS	(no)	(no)		
Discrete data	yes	yes		
Variable length patterns	no	yes		
Multi-type TS	yes	no		
Continuous data	no	no		
Pre-processing	O(k)	-		
Context durations	no	no		
Continuous time	no	no		