

# Algorithmen und Datenstrukturen II

## Übung 1

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# Dynamic Programming

**Overlapping Subproblems**

**Optimal Substructure**

**Memoization**

Fibonacci-Zahlen

**Dynamic  
Programming**

Longest Common  
Subsequence

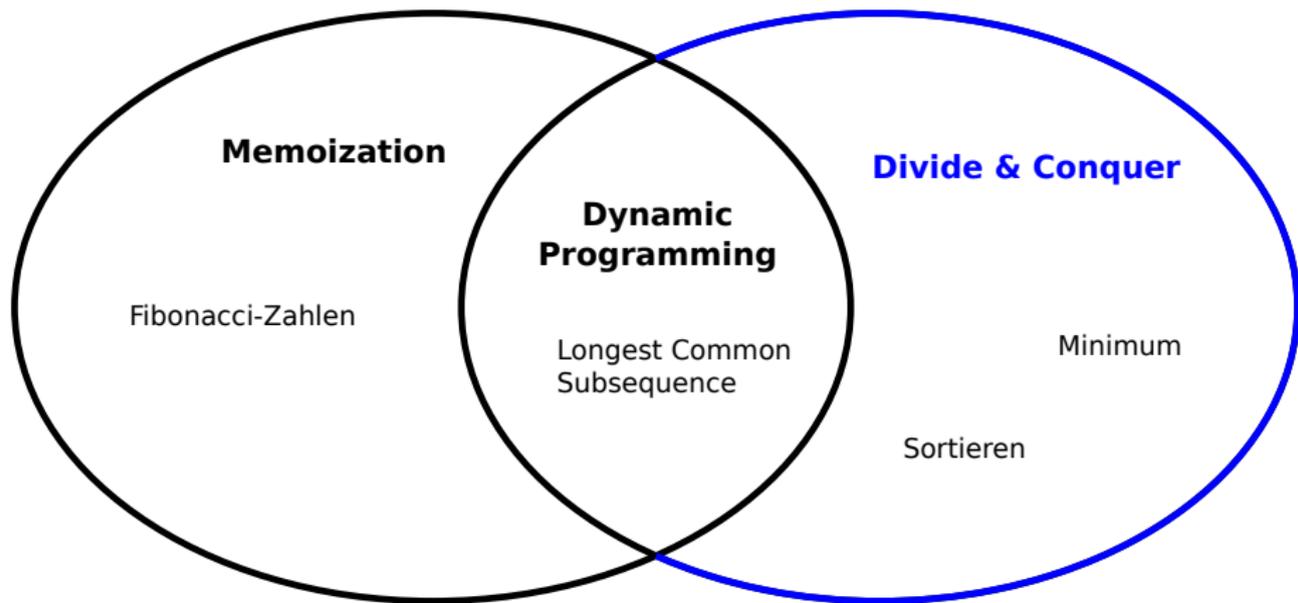
**Divide & Conquer**

Minimum

Sortieren

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## Algorithmus 1 – Rekursiv

$$F_0 = 0$$

$$F_1 = 1$$

$$F_i = F_{i-1} + F_{i-2} \text{ für } i \geq 2$$

```
function FIB(i)  
  if i ≤ 1 then  
    return i  
  else  
    return FIB(i - 1) + FIB(i - 2)  
  end if  
end function
```

## Algorithmus 2 – Top-Down

$$F_0 = 0, F_1 = 1, F_i = F_{i-1} + F_{i-2} \text{ für } i \geq 2$$

**function** FIB( $i$ )

$F \leftarrow \text{array}[0 \dots i]$

$F[0] \leftarrow 0$

$F[1] \leftarrow 1$

$F[2] \leftarrow \dots \leftarrow F[i] \leftarrow \infty$

**return** FIB\_HELP( $i, F$ )

**end function**

**function** FIB\_HELP( $i, F$ )

**if**  $F[i] = \infty$  **then**

$F[i] \leftarrow \text{FIB\_HELP}(i - 1, F) + \text{FIB\_HELP}(i - 2, F)$

**end if**

**return**  $F[i]$

**end function**

## Algorithmus 3 – Bottom-Up

```
function FIB( $i$ )  
  if  $i \leq 1$  then  
    return  $i$   
  else  
     $f_{\text{prev}} \leftarrow 0$   
     $f \leftarrow 1$   
    for  $k \leftarrow 2, \dots, i$  do  
       $f_{\text{next}} \leftarrow f + f_{\text{prev}}$   
       $f_{\text{prev}} \leftarrow f$   
       $f \leftarrow f_{\text{next}}$   
    end for  
  end if  
  return  $f$   
end function
```

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## Algorithmus 4

```
function LCS( $a_1 \dots a_n, b_1 \dots b_m$ )  
   $C \leftarrow$  array[ $0 \dots n$ ][ $0 \dots m$ ]  
   $C[0, 0] \leftarrow \dots \leftarrow C[n, 0] \leftarrow 0$   
   $C[0, 1] \leftarrow \dots \leftarrow C[0, m] \leftarrow 0$   
  
  for  $i \leftarrow 1 \dots n$  do  
    for  $j \leftarrow 1 \dots m$  do  
      if  $a_i = b_j$  then  
         $C[i, j] \leftarrow C[i - 1, j - 1] + 1$   
      else  
         $C[i, j] \leftarrow \max \{ C[i - 1, j], C[i, j - 1] \}$   
      end if  
    end for  
  end for  
  return  $C[n, m]$   
end function
```

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