Synchronizers, Arbiters, GALS and Metastability

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Outline

- What’s the problem? Why does it matter?
- Time and distributions
- Noise – decisions are not deterministic.
- Synchronizer latency, can it be avoided?
- Measuring and some interesting effects
What’s the problem: The digital IP world and the rest of the world

The synchronizer is the guy that allows timing flexibility

Everything else, or Reality

Your system

The synchronizer is the guy that allows timing flexibility
Synchronizers and arbiters

- **Synchronizer**
  Decides which clock cycle to use for the input data

- **Asynchronous arbiter**
  Decides the order of inputs
Time Comparison Hardware

- Digital comparison hardware (which compares integers) is easy
  - Fast
  - Bounded time

- Analog comparison hardware (which compares reals like time) is hard
  - Normally fast, but takes longer as the difference becomes smaller
  - Can take forever, (Buridan’s Ass ~1340)

- Synchronization and arbitration involve comparison of time

- Known to early computer designers:
  - Lubkin 1952, Catt 1966
  - Chaney and Littlefield 1966/72
Asynchronous Network (Sparsø, ASYNC 2005)

- Sparsø
  - Synchronization required
  - Multiple Clocks
  - Arbitration required

Diagram:
- IP block
- Network adapter
- Routing node
- Packet switching fabric
- Distributed shared memory
- OCP interfaces
- Multiple Clocks
- Synchronization required
- Arbitration required
Synchronization of data

- Non pausible clocks require data synchronization
- You have a limited time to synchronize.
- Synchronizer circuits may fail to work in that time
- System sometimes fails (you fly into a mountain)
- Synchronization time = latency
Synchronization of clocks

- Clock paused to prevent contention
- Wait for MUTEX output to resolve
- Can take forever (with decreasing probability)
- This may not be acceptable (you fly into a mountain)
Trends

- Communications are limiting performance
- Difficulty (Impossibility?) in maintaining one clock per chip
- Need reduce wasted power in clocks
- Timing closure problems
  - Interconnect delay times long
  - Variability increases
- Move towards asynchronous networks
Metastability is....

Set-up time violated

Request

\( \Delta t_{in} \)

Processor Clock

\( \Delta t_{in} \rightarrow 0 \)

Not being able to decide...

\( Q \)

Clock

\( D \)

\( Q \)
Metastability in a Latch

Stable points

Metastable Point
Simple Linear Model

- Simple linear model leads to two exponentials
- \( \tau_a \) is convergent, \( \tau_b \) is divergent

\[
\begin{align*}
\tau_1 &= \frac{C_1 \cdot R_1}{A}, \quad \tau_2 = \frac{C_2 \cdot R_2}{A} \\
g_m &= \frac{A}{R} \\
0 &= \tau_1 \cdot \tau_2 \cdot \frac{d^2 V_1}{dt^2} + (\tau_1 + \tau_2) \cdot \frac{dV_1}{dt} + \left( \frac{1}{A^2} - 1 \right) V_1 \\
V_1 &= K_a e^{-\tau_a t} + K_b e^{\tau_b t}
\end{align*}
\]
Synchronizer

- \( t \) is time allowed for the Q to change between CLK a and CLK b
- \( \tau \) is the recovery time constant, usually the gain-bandwidth of the circuit
- \( T_w \) is the “metastability window”
- \( \tau \) and \( T_w \) depend on the circuit
- We assume that all values of \( \Delta t_{in} \) are equally probable

\[
MTBF = \frac{e^{t/\tau}}{T_w \cdot f_c \cdot f_d}
\]
Typical responses

- All starting points are equally probable
- Most are a long way from the “balance point”
- A few are very close and take a long time to resolve
Event Histogram

The slope is \(-1/\tau\)

Log Probability of event depends on \(\Delta\) time

The intercept is \(\sim T_w\)

- Propagation delay

Events

Propagation delay

Normal delay
Synchronizer state of the art

- You require about 35 $\tau$ s in order to get the MTBF out to about 1 century. (That’s for 1 synchronizer)
- There is nothing else you can do while synchronizing
- Each typical static gate delay is equivalent to about 5 $\tau$ Synchronizers are analog devices, so worse affected by scaling
- Bigger SoCs, in future systems so more synchronizers, worse reliability
- Inputs can be ‘malicious’ i.e. always causing metastability.
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The arbiter (MUTEX)

- Asynchronous arbitration, No time bound
- Seitz metastability filter
- Grants cannot occur until after the latch resolves any metastability
Arbitration time

- Unlike a synchronizer, an arbiter may take for ever.
- It usually doesn’t, long responses are rare.
- On average the time should only be $\tau$ longer than the normal response, so DEAD time ought to be low.
- Outputs are always monotonic.

![Diagram showing request and grant timelines with $t_m$ mark]
Gate metastability filter

- Half levels due to metastability need to be removed
  - Low (or high) threshold inverters
  - Measure divergence
- Filters define the time to reach a stable state

\[
V_t = \frac{V_{dd}}{4}
\]

\[
\frac{V_{dd}}{2}
\]

\[
\frac{V_{dd}}{2}
\]
Resolution time can be affected

- The start/finish points make a difference
- Grant appears when trajectory crosses the filter threshold
- Gate metastability filter shows more variation
- Seitz filter shows more delay
Event distribution

- Assumption: Time between two events (R1 and R2) is evenly distributed.
- Typically it is not.
- Can be as much as 7:1 variation.
- Here there are more cases where R1 is just after R2.
- Arbitration may not be fair.
Non uniform probabilities and time

- Time for metastability averaged over a distribution $T$ in a MUTEX is:

$$\text{Average}_\text{time} = \tau \int_{0}^{T} \ln \left( \frac{T_w}{\Delta t_{in}} \right) d\Delta t_{in}$$

- If $T = \infty$, $\text{Average}_\text{time} = \tau$

BUT

For a malicious input, distribution limited by noise

- If $T = 4ps$, $T_w = 25ps$, $\text{Average}_\text{time} = 4 \tau$

- Noise can sometimes make average time faster
Predicting performance

- MUTEX circuits are fast

- BUT delay times may not be easy to predict
  - Cannot rely on ALL times being fast

- Synchronizers are known to be unreliable
Future processes

- Synchronizers and arbiters don’t work well in nanometre technologies, especially at low Vdd
- Worse that gates! Why?
- A gate input is either HIGH
  - Output pulled down
- Or LOW
  - Output pulled up
- A metastable gate is neither
  - Both transistors can be off
- Vdd decreases with process shrink,
  - $g_m$ very low
- Synchronization time constant $\tau = C/g_m$
Robust synchronizer

- Jamb latch synchronizer slow for low $V_{dd}$, low temp
- In metastability, both outputs are the same
- Extra p-types are switched fully on, so $g_m$ increases, and $\tau$ improves
## Results

\[ \tau (\text{metastability time constant}) \text{ vs } \text{Vdd} \]

<table>
<thead>
<tr>
<th>Vdd(v)</th>
<th>Jamb Latch B</th>
<th>Robust Synchronizer</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.8</td>
<td>35.55</td>
<td>34.92</td>
</tr>
<tr>
<td>1.7</td>
<td>37.29</td>
<td>35.76</td>
</tr>
<tr>
<td>1.6</td>
<td>40.93</td>
<td>38.25</td>
</tr>
<tr>
<td>1.5</td>
<td>52.36</td>
<td>43.07</td>
</tr>
<tr>
<td>1.4</td>
<td>66.17</td>
<td>50.36</td>
</tr>
<tr>
<td>1.35</td>
<td>75.35</td>
<td>58.19</td>
</tr>
</tbody>
</table>
Outline

• What’s the problem? Why does it matter?
• Time and distributions
• Noise – decisions are not deterministic.
• Synchronizer latency, can it be avoided
• Measuring and some interesting effects
Does noise affect $\tau$?

- Probability of escape from metastability does not change with gaussian noise (Couranz and Wann 1975)
Does noise affect $\tau$?

- Probability of escape from metastability does not change with gaussian noise (Couranz and Wann 1975)

![Trajectories graph](image)
Can noise change the failure rate?

Or maybe not.....
The normal case

- Probability of initial difference due to noise component $P_1(v)$
- Probability of initial difference due to input clock data overlap $P_0(v)$
- Convolution
- Result of convolution $P(v)$
The malicious input

Probability of initial difference due to noise component $P_1(v)$

Probability of initial difference with zero input clock data overlap $P_0(v)$

Result of convolution $P(v)$
Non-determinism

- Synchronizers and arbiters can produce non-deterministic outcomes
- Some noise is deterministic (5-50ps)
  - Power supply, crosstalk
- Some noise is non-deterministic (typically 0.1ps - 0.5ps).
  - Thermal noise, which increases as dimensions reduce.
- Sequence and time of an individual computation paths is unpredictable
- System performance can only be predicted probabilistically
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Request and Acknowledge

Data Available

Write Clocks

ACK

D Q

D Q

DATA

D Q

D Q

Read Clocks

Read done

Data Available

Request and Acknowledge

Write Clocks

Acknowledgment

Read Clocks

Read done
Latency

- It takes one - two receive clocks to synchronise the request
- Then one – two write clocks to acknowledge it
- Significant latency (1-3 clocks)
- Poor data rate (2 – 6 Clocks)
FIFO

- Can improve data rate by using a FIFO
- But not latency (which gets worse)
- FIFO is asynchronous (usually RAM + read and write pointers)
Timing regions can have predictable relationships

- **Phase locked** (*mesochronous*)
  - Timing of input data is constant, therefore predictable

- **Same or related frequencies but phase difference can drift in an unbounded manner.** (*plesiochronous*)
  - Timing is not constant but is still predictable

- **Unrelated frequencies** (*Heterochronous*)
  - No assumptions about timing can be made
  - Need a synchronizer
Don’t synchronise when you don’t need to

- If the two clocks are locked together, you don’t need a synchroniser, just an asynchronous FIFO big enough to accommodate any jitter/skew
- FIFO must never overflow/underflow, so there is latency

![Diagram of a FIFO with inputs and outputs](image)
Mesochronous data exchange

- Intermediate X register used to retim data
- Need to find a place where write data is stable, and read register available. There is always a place which can be found at start up
  - Chakraborty and Greenstreet ASYNC 2003
Clock delay synchronizer (Ginosar AINT 2000)

conflict region
Delay synchronizer latency

- Nominally 0 – 1 clock cycle
- Relies on accurately predicting conflicts
- Clocks must remain stable over synchronisation time.
- Always lose $t_{ko}$ of next computation stage
- Alternative: shift all conflicts to next read cycle
  - On average this loses 2d
  - 2d must be big enough to cover any clock drift/jitter over synchronization time
Speculation

- Mostly, the synchronizer does not need $30\tau$ to settle
- Only $e^{-13}$ (0.00023%) need more than $13\tau$
- Why not go ahead anyway, and try again if more time was needed
Low latency synchronization

- Data Available, or Free to write are produced early.
- If they prove to be in error, synchronization failed.
- Read Fail or Write Fail flag is then raised and the action can be repeated.
When to recover

Early Data Available is set after a half cycle – 2 inverter delays
Speculative Data Available after a half cycle
If these two are different at end of cycle, set Fail

<table>
<thead>
<tr>
<th>1. Early Half Cycle - 2τ</th>
<th>2. Speculative Half Cycle</th>
<th>Final End of Cycle</th>
<th>Fail 1 &amp; 2 different End of Cycle</th>
<th>Comment</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>No data was available</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>Stable at the end of the cycle, but the speculative output may have been metastable. Fail</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>Normal data Transfer</td>
</tr>
</tbody>
</table>
Synchronizer latency reduction

1. Only have one clock for the whole system
2. Use clocks with a predictable relationship
3. Speculate
4. Synchronise at the start of a burst transfer, the data rate is predictable during the burst
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What we know about metastability

- Things we know
  - Synchronizers are unreliable, the more there are the more unreliable the system
  - How to measure reliability up to a few hours

- Things we know we don’t know
  - What reliability is at 3 years
  - How to measure it
  - Complex circuits give complex results, the simple MTBF formula may not apply

- Things we don’t know we don’t know
  - What happens on the back edge of the clock
- Slope, $\tau$, is about 120ps (in fast region)
- Typical delay time (most events) is 4ns
- 99.9% of clock cycles do not cause useful events
- To get 1 event at 7ns requires hours
Increasing the number of events

- Test FF is driven to metastability
- Every clock produces a metastable response
- Integrator ensures half outputs high, half low

```
10 MHz

Variable Delay

Integrator

D Test FF Q

D Slave FF Q
```
What you get

- Clock to D (Input) histogram
- Q to Clock (Output) histogram
Interpreting results

Input time distribution is not flat
Proportion of total inputs causing events vs input time
Proportion of total output events vs output time
Mapping output times to input times

0 < Balance point > 1

Input time distribution is not flat
Proportion of total inputs causing events vs input time
Proportion of total output events vs output time
Mapping output times to input times
Results

- $\Delta_t$ is the time from the “balance point” of ~200ps
- Similar to original graph BUT not events
- Orders of magnitude quicker to gather data
- Reliability for days not minutes
- Only one oscillator, so no distribution issues
- $\Delta_t$ does not depend on $f_c$ and $f_d$ or measurement time. Events do

$$
\Delta_t = T_w e^{\frac{-t}{\tau}}
$$

$$
MTBF = \frac{1}{\Delta_t f_c f_d}
$$
When the clock goes low

- Clock goes high, master goes metastable
- Master output arrives at slave
  - Before slave clock high: transparent gate delay $t_d$
  - As slave clock goes high: metastable, slightly longer delay

Back edge of clock causes increased delay
Effect of clock low on 74F5074

- 1 – 3 ns additional delay
Measurement results

- Reliability measurements extended from
  - $10^{-15}$ s or MTBF = 16 min at 10MHz, to
  - $10^{-22}$ s or MTBF = 3 years

- We can see variations in $\tau$ not previously seen

- Measurement is statistical, not affected by noise

- Not affected by oscillator linking

- Back edge of clock pulse is seen to be an important effect, can be $0 - 15\tau$
Conclusions

- Synchronization/arbitration requires special circuit elements
- They’re not digital!
- Well known models of synchronizers and arbiters exist
- Design gets more difficult with small dimensions
- Synchronizers and arbiters are not deterministic.
- Both circuits and systems may not conform to idealized models
- Differences can lead to poor reliability, unfair arbitration, and unpredictable performance